

# APPLICATION OF A LOCALITY PRESERVING DISCRIMINANT ANALYSIS APPROACH TO ASR

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# Outline

- ▶ **Background:** Feature analysis for HMM (hidden Markov model) based ASR
- ▶ **Problem:** Capturing spectral dynamics requires high dimensional feature vectors ( $\text{dim} > 100$ , typically)
- ▶ **Solution:** Dimensionality reducing linear transformations
- ▶ **Approach:** Locality preserving discriminant analysis (LPDA)
  - ▶ maximize discrimination between model classes
  - ▶ preserve local structure of the within-class data
- ▶ **Experimental Study:** Compare ASR performance for a speech in noise task using LPDA with performance obtained using more well known approaches

# ASR Feature Analysis

## ▶ Mel-frequency Cepstrum Coefficients (MFCC)



- ▶ Captures the static spectral information over a  $\sim 20$  msec analysis frame.
- ▶ What about surrounding speech context (evolution of speech spectrum)?

# Capturing Spectrum Evolution

- ▶ Concatenate multiple speech frames (typically  $\sim 100$  msec of speech):

$$\mathbf{x}_i = \begin{bmatrix} \bar{\mathbf{x}}_{i-k} \\ \vdots \\ \bar{\mathbf{x}}_i \\ \vdots \\ \bar{\mathbf{x}}_{i+k} \end{bmatrix}$$

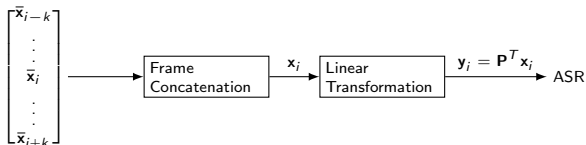
[Eisele and Haeb-Umbach, 1996]

- ▶ Issues:
  - ▶ High dimensionality of the resultant feature vectors ( $dim = \mathbf{117}$  for  $k = \mathbf{4}$ )
  - ▶ High inter-frame correlation among feature vectors
- ▶ **Solution:** Dimensionality reducing linear transformations

# Feature-space Transformations

- ▶ Project high dimensional feature vectors to a lower dimensional space

$$\mathbf{y}_i = \mathbf{P}^T \mathbf{x}_i$$



- ▶ Optimization criteria for estimating  $\mathbf{P}$ :
  - ▶ Improved class separability – use a discriminant criterion
    - Linear Discriminant Analysis (LDA) [Duda et al., 2000]
  - ▶ Preserve underlying geometrical relationships among the feature vectors – use a manifold learning approach
    - Locality Preserving Projections (LPP) [He and Niyogi, 2002, Tang and Rose, 2008]

# Manifold Learning

- ▶ Find a low-dimensional basis for describing high dimensional data
- ▶ Assumption: High dimensional data can be considered as a set of geometrically related points resting on or close to the surface of a lower dimensional manifold.
- ▶ **Why:** Local relationships among feature vectors can be constrained by the manifold

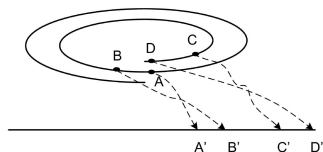


Illustration of dimensionality reduction for two-dimensional data embedded in a nonlinear manifold space with relative position information reserved. [Tang and Rose, 2008]

# An Alternative Optimization Criterion

- ▶ Motivation:
  - ▶ Discriminant approaches like LDA do not account for the geometric structure of the data
  - ▶ Locality preserving approaches like LPP do not enhance class discrimination
- ▶ Locality preserving discriminant approach (LPDA):
  - Combines manifold learning with inter-class discrimination
  - Multiple class specific sub-manifolds
    - ▶ Maximize class separability : Discriminate between sub-manifolds
    - ▶ Preserve local within class relationships : Preserve local sub-manifold structures

# Locality Preserving Discriminant Analysis (LPDA)

- ▶ Embed feature vectors  $\mathbf{X}$  into graph(s)  $\mathcal{G}$  defined over *some* geometric measure  $\mathbf{W} = [w_{ij}]_{N \times N}$  [Yan et al., 2007]
  - ▶ The idea is to manipulate the geometry of the graph nodes while preserving important relationships between them
- ▶ For a graph  $\mathcal{G} = \{\mathbf{X}, \mathbf{W}\}$ , graph scatter measure in the transformed space is defined as:

$$F(\mathbf{P}) = \sum_{i \neq j} \|\mathbf{y}_i - \mathbf{y}_j\|^2 w_{ij} = \sum_{i \neq j} \|\mathbf{P}^T \mathbf{x}_i - \mathbf{P}^T \mathbf{x}_j\|^2 w_{ij}$$

The goal of LPDA is to minimize the within class scatter, and maximize the between class scatter while preserving local relationships



# LPDA – Graph Embedding

- ▶ Embed the feature vectors belonging to the same class into intrinsic graph  $\mathcal{G}_{int} = \{\mathbf{X}, \mathbf{W}_{int}\}$ 
  - ▶  $\mathbf{X}$  = Nodes of the graphs = features vectors
  - ▶  $\mathbf{W}_{int}$  = Intrinsic affinity matrix;  $\mathbf{W}_{int} = [w_{ij}^{int}]_{N \times N}$

$$w_{ij}^{int} = \begin{cases} \exp(-\|\mathbf{x}_i - \mathbf{x}_j\|^2)/\rho & ; \text{ } \mathbf{x}_i \text{ \& } \mathbf{x}_j \text{ are close and in same class} \\ 0 & ; \text{ otherwise} \end{cases}$$

- ▶ Embed the feature vectors belonging to different classes into penalty graph  $\mathcal{G}_{pen} = \{\mathbf{X}, \mathbf{W}_{pen}\}$ 
  - ▶  $\mathbf{W}_{pen}$  = Penalty affinity matrix;  $\mathbf{W}_{pen} = [w_{ij}^{pen}]_{N \times N}$

$$w_{ij}^{pen} = \begin{cases} \exp(-\|\mathbf{x}_i - \mathbf{x}_j\|^2)/\rho & ; \text{ } \mathbf{x}_i \text{ \& } \mathbf{x}_j \text{ are close but NOT in same class} \\ 0 & ; \text{ otherwise} \end{cases}$$

## LPDA – Optimization Criterion

- ▶ Minimize the scatter of the intrinsic graph  $F_{int}(\mathbf{P})$  (preserve within-class manifold based relationships)
- ▶ Maximize the scatter of the penalty graph  $F_{pen}(\mathbf{P})$  (maximize inter-class discrimination)

$$\mathbf{P}_{lpda} = \arg \max_{\mathbf{P}} \frac{F_{pen}(\mathbf{P})}{F_{int}(\mathbf{P})}$$

- ▶  $\mathbf{P}_{lpda}$  can be obtained by solving the generalized eigenvalue problem:

$$(\mathbf{X}(\mathbf{D}_{pen} - \mathbf{W}_{pen})\mathbf{X}^T)\mathbf{p}_{lpda}^j = \lambda_j(\mathbf{X}(\mathbf{D}_{int} - \mathbf{W}_{int})\mathbf{X}^T)\mathbf{p}_{lpda}^j$$

$\mathbf{D} = [d_{ij}]$  is a diagonal matrix whose elements correspond to the column sum of the affinity matrix  $\mathbf{W}$ , e.g.,  $d_{ii}^{int} = \sum_j w_{ij}^{int}$  etc.

# Experimental Study

- ▶ Evaluate feature-space dimensionality reducing transformations in terms of ASR word error rate (WER) on a speech in noise task domain
- ▶ Compare:
  - ▶ Linear discriminant analysis (LDA)
  - ▶ Locality preserving projections (LPP)
  - ▶ Locality preserving discriminant analysis (LPDA)
- ▶ After projection, feature-decorrelation (diagonal covariances) is no longer guaranteed
  - ▶ Most ASR systems assume diagonal covariances
  - ▶ Combine with semi-tied covariance (STC) transformations

[Gales, 1999]

# Task Domain

- ▶ Aurora2 speech corpus:
  - ▶ 8440 noise corrupted utterances from 55 male and 55 female speakers for training
  - ▶ 4004 utterances; four different noise types for testing
- ▶ Baseline:
  - ▶ 12-dimensional MFCC + Energy +  $\Delta$  +  $\Delta\Delta$  features used for baseline
  - ▶ Whole word continuous density HMM model
  - ▶ 11 words + sil + sp, 16 states per word  $\Rightarrow$  180 states, 3 Gaussians per state
- ▶ Feature-space transformations:
  - ▶ 9 frames stacked for feature concatenation
  - ▶ Continuous density HMM states used as classes
  - ▶ Semi-tied covariance adaptation is performed

## ASR (% WER) for Aurora2 Corpus

Noise Type	Technique	SNR (dB)			
		20	15	10	5
Car	Baseline	2.77	3.36	5.45	<b>12.31</b>
	LDA	3.82	4.26	6.74	17.15
	LDA + STC	2.83	3.45	5.69	15.92
	LPP+STC	2.71	3.61	6.08	14.97
	LPDA+STC	<b>2.30</b>	<b>2.77</b>	<b>5.19</b>	12.73
Airport	Baseline	3.42	4.88	8.49	16.58
	LDA	5.67	7.07	10.26	19.83
	LDA+STC	3.18	4.11	7.72	15.65
	LPP+STC	4.35	6.95	10.38	21.15
	LPDA+STC	<b>3.10</b>	<b>4.09</b>	<b>7.49</b>	<b>15.09</b>

- ▶ Use of semi-tied covariance (STC) is critical for all approaches.

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- ▶ All approaches are effective (better than baseline) at high and medium SNR's
- ▶ All approaches are not effective at low SNR

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- ▶ LPDA+STC provides highest WER reduction in most noise conditions

## Conclusions

- ▶ LPDA: a feature-space dimensionality reduction approach that combines discriminant and manifold learning criteria



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  - ▶ Graph embedding:
    - ▶ A generalized framework
    - ▶ No assumption about the distribution of data
  - ▶ Manifold learning: Preserve within-class nonlinear structure of the data
  - ▶ Between class discrimination
  - ▶ Soft-weights: the closer the two vectors the higher the penalty upon misclassification

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  - ▶ Soft-weights: the closer the two vectors the higher the penalty upon misclassification
- ▶ Provides from 6 – 27% reduction in WER relative to LDA
- ▶ Populating the affinity matrices  $\mathbf{W}_{int}$  and  $\mathbf{W}_{pen}$  is a very computationally intensive task
  - ▶ Future work will include reducing the relatively high computation cost of estimating the LPDA transformation matrix

# References



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# Why STC?

- ▶ Only a limited number of parameters can be *robustly* estimated for each CDHMM state
  - ▶ Modeling full covariances (when correlation exists) results in a dramatic increase in such parameters
  - ▶ Hence, independence between feature vector components is assumed in ASR
  - ▶ But not explicitly modeling the full-covariance results in ASR performance degradation
- ▶ Dimensionality reduction generally results in a highly correlated feature space, *i.e.*, full covariance matrices
  - ▶ Discarding this information results in performance degradation
- ▶ Semi-tied covariances [Gales, 1999]:
  - ▶ Approximates full covariance modeling by allowing few full covariance matrices to be shared across many distributions
  - ▶ Effectively each distribution maintains its own diagonal covariance